# Kalman Filtering for Real-Time Individual Cylinder Air Fuel Ratio Observer on a Diesel Engine Test Bench

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Abstract—We propose an estimator of the individual cylinder air fuel ratios in a turbocharged Diesel Engine using as only sensor the single air fuel ratio sensor placed downstream the turbine. The observer consists of a time-varying Kalman Filter based on a physics-based model for the engine dynamics. We prove that the reference system converges toward a limit cycle. This limit cycle is used for the design of an extended Kalman filter. Performance is evaluated through test bench experiments on a 4 cylinder Diesel engine. The proposed approach has the advantage over existing methods of providing insight into the cylinders unbalance by considering a higher frequency model of the exhaust manifold. This information could pave the road to efficient closed loop control strategy as demonstrated on an experimental example.

#### I. Introduction

As the performance and environmental requirements have continued to rise over the years, the interest in advances control strategies for automotive applications has increased. In this context, controlling the combustion represents a key challenge being examined by numerous research teams [1], [2] and references therein. Among many, several tentative solutions are combustion torque control and estimation (see for example [3], [4], [5] and [6]), Air Fuel Ratio control and estimation (see [7], [8] and [9]),.... The control of the *individual* Air Fuel Ratio (AFR: the weight ratio of air-to-gasoline), which is a good representation of the torque balance of the engine, has emerged as an important step.

Classically, in spark ignition engines, overall AFR is directly controlled with the injection system. By this control strategy, all cylinders share the same closed-loop input signal based on the single  $\lambda$ -sensor, an oxygen sensor in the exhaust manifold  $\lambda \triangleq 1 - \frac{M_{aix}}{M_T}$  providing, under lean operating conditions, a direct reading of the normalized Fuel Air Ratio (FAR) measurement [10, chap. 3], and thus of the AFR. Ideally, all the cylinders should have the same AFR as they have the same injection set-point. Unfortunately, due to inherent flaws of the injection system (such as pressure waves and mechanical tolerances), the total mass of fuel injected in each cylinder is very difficult to predict with a relative precision below 7%. This lack of precision results in non optimal engine operating conditions. Consider now a class of planned Homogeneous Charge Compression Ignition (HCCI)

engines, referring to [11], [12], [13], [14] for an overview of the technology, [15], [16], [17] for more control oriented models, and [18], [19], [20], [21], [22] for control techniques. For these engines and regeneration filters (Particulate filters,  $DeNO_x$  [23], [24], [25], even slight unbalance between the cylinders can in particular induce malicious noise, possible stall and increased emissions. Cylinder-individual control is needed to address the potential drawbacks in these planned technologies. In this context, *cylinder-individual* AFR estimation may provide crucial information to assist the HCCI engine controller. This is the focus of the paper.

In previous published works (see [26] and [27]), the methods used to reconstruct the AFR of each cylinder from the UEGO (Universal Exhaust Gas Oxygen) sensor measurement are based on the permutation dynamics at the TDC (Top-Dead Center) sample angle and a gain identification technique. The requirement we perceive as being critical for efficient control strategies is a high frequency estimation of the individual cylinder AFR:  $6^o$  sample angle estimation instead of  $90^o$  (TDC). We design an observer on the balance model of the exhaust manifold. We use a physics-based model underlying the role of periodic input flows (gas flows from the cylinders into the exhaust manifold).

The contribution of this paper is the design and experimental validation of a real-time high frequency observer based on an extended Kalman filter. Tests are conducted on a four cylinder turbocharged diesel test bench presented in [28]. We stress that this observer is relevant for application purposes by illustrative torque balancing closed loop results.

The paper is organized as follows. In Section II, we present the physics-based model of the exhaust manifold. We prove that the continuous-time dynamics converges toward a limit cycle ( $x_{per}$ ). In Section III, using this limit cycle, we derive a periodic linear discrete-time model that serves as a reference for a proposed Kalman filter. This discrete-time model is a discrete approximation of continuous-time dynamics by an Euler explicit scheme around the limit cycle  $x_{per}$ . Implementation and experimental results are reported in Section IV. Finally, future directions are given in Section V.

## II. EXHAUST MANIFOLD MODEL

Figure 1 depicts the flow sheet of the individual AFR from the cylinders outlet down to the turbine, where the sensor is located at. From the cylinders to the AFR sensor (located downstream the turbine) the gases travel through the exhaust pipes, the exhaust manifold and the turbocharger.

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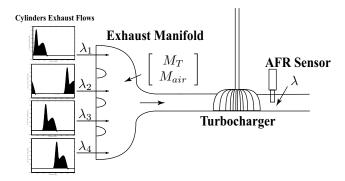


Fig. 1. Individual Air-Fuel Ratio problem: a single sensor located downstream the turbine is available to reconstruct individual AFR.

The AFR can be rewritten, neglecting EGR, as

$$\lambda \triangleq 1 - \frac{M_{air}}{M_T}$$

The various AFR have an influence on the gas pressure, temperature, and composition in the exhaust manifold. In a very naive model, the gases move at constant speed, without mixing. In practice, diffusion and mixing effects are present. Therefore, we propose a nonlinear model to take these into account. Our approach focuses on macroscopic balances involving experimentally derived nonlinear functions.

## A. Mass balance in the exhaust manifold

Balance equations are described by (1) and (2). We assume that the individual AFR are constant about a given setpoint. The sensor dynamics is represented as a first order dynamics (3)

$$N_e \frac{dM_T}{d\alpha} = \sum_{i=1}^{n_{cyl}} d_i(\alpha, \Xi) - d_T(M_T, \Xi) \tag{1}$$

$$N_e \frac{dM_{air}}{d\alpha} = \sum_{i=1}^{n_{cyl}} (1 - \lambda_i) d_i(\alpha, \Xi) - \frac{M_{air}}{M_T} d_T(M_T, \Xi) \quad (2)$$

$$N_e \frac{d\lambda_{mes}}{d\alpha} = \frac{1}{\tau} \left( \frac{M_T - M_{air}}{M_T} - \lambda_{mes} \right) \tag{3}$$

$$N_e \frac{d\lambda_i}{d\alpha} = 0, \ \forall i \in [1, \ n_{cyl}]$$
 (4)

Notations are given in Table I. Operating conditions are defined by the  $\Xi$  parameters (mean aspirated flow  $D_{asp}$ , exhaust temperature  $T_{exh}$ , turbocharger speed  $N_{turbo}$ ). They are considered constant over an engine cycle.

The  $T_0$ -periodic  $d_i(.,\Xi)$  functions are modelled through interpolation of a large number of available data. The functions family  $\{d_i\}_{i=1...n_{cyl}}$  is a linearly independent family of the set of continuous  $T_0$ -periodic functions.

The flow rate through the turbine  $d_T$  is a function of the total mass  $M_T$ , smooth away from 0, and can be factorized as

$$d_T(M_T, \Xi) = p(M_T, \Xi)M_T$$

where p is a positive increasing (concave) function with respect to the total mass  $M_T$ , e.g.  $p(z, \Xi) =$ 

TABLE I NOMENCLATURE.

Symb.	Quantity	Unit
$\alpha$	Crankshaft angle	
$M_T$	Total mass of gas in the exhaust manifold	kg
$M_{air}$	Mass of air in the exhaust manifold	kg
$N_e$	Engine Speed	rpm
$d_T$	Gas flow rate through the exhaust manifold	$kg.s^{-1}$
$d_i$	Gas flow rate from cylinder i	$kg.s^{-1}$
Ξ	Operating conditions	
$D_{asp}$	Mean aspirated flow	$kg.s^{-1}$
$T_{exh}$	Temperature in the exhaust manifold	$^{o}\mathrm{K}$
$N_{turbo}$	Turbocharger speed	rpm
r	EGR rate	
$\lambda_i$	Normalized Fuel-Air Ratio of cylinder i	
$\lambda$	Oxygen sensor measurement	
P	Pressure in the exhaust manifold	bar
$z_0$	Total mass in the exhaust manifold kg	
	under atmospherical conditions	
$n_{cyl}$	Number of cylinders	
$\lambda_{i,ref}$	Reference normalized Fuel-Air Ratio	
	of cylinder i	
$\Delta \alpha \triangleq \frac{\pi}{30}$	Angular sample time	
$T_0 \triangleq 4\pi$	Period of the continuous-time dynamics	
$N_0 \triangleq 120$	Period of the discrete-time dynamics	
$\delta \triangleq \frac{\Delta \alpha}{N_e}$	Constant	$\rm rpm^{-1}$

 $p_0(\Xi)\sqrt{2\frac{\gamma}{\gamma-1}((\frac{z}{z_0})^{-\frac{2}{\gamma}}-(\frac{z}{z_0})^{-\frac{\gamma+1}{\gamma}})}$ . Usually given by a 2D look up table, the flow rate is modelled as a flow through a restriction, as in [10], whose section depends on the pressure ratio and the turbocharger speed (as proposed in [29] and [30]). Composition of the flow through the turbine and in the exhaust manifold are considered equal.

The measurements are

- P the pressure in the exhaust manifold assumed to be related to the total mass by  $P = \gamma_T M_T$  with  $\gamma_T \triangleq \frac{RT_{exh}}{V_{exh}}$  considered as a constant over an engine cycle.
- $\lambda_{mes}^{res}$  the Air Fuel Ratio measurement.

## B. The masses dynamics converge toward a limit cycle

First, we prove that the exhaust dynamics are a periodically driven contracting system. Then, the Kalman filter is defined in the vicinity of the limit cycle. Total and air masses balance equations (1) and (2) can be written under the form

$$\frac{dM}{d\alpha} = g(\alpha) - f_{\Xi}(M) \tag{5}$$

where  $M = \begin{bmatrix} M_T & M_{air} \end{bmatrix}^T$ ,  $f_\Xi(M) = \frac{1}{N_e} \begin{bmatrix} M_T p(M_T,\Xi) & M_{air} p(M_T) \end{bmatrix}^T$  and  $g(\alpha) = \frac{1}{N_e} \sum_{i=1}^{n_{cyl}} d_i(\alpha,\Xi) \begin{bmatrix} 1 & (1-\lambda_i) \end{bmatrix}^T$ . Let  $D \triangleq \{(M_T,M_{air}) \in (\mathbb{R}^+)^2 & M_T \geq M_{air} \text{ and } M_T > (1+\epsilon)M_0 & \epsilon > 0\}$ . For all  $(M_T,M_{air}) \in D$ ,

$$N_e \frac{d(M_T - M_{air})}{d\alpha} = (M_T - M_{air})p(M_T, \Xi) + \sum_{i=1}^{n_{cyl}} \lambda_i d_i(\alpha, \Xi) > 0$$

and  $\frac{dM_T}{d\alpha} \geq 0$  because,  $\forall \alpha, \sum_{i=1}^{n_{cyl}} d_i(\alpha, \Xi) > (1 + \epsilon) M_0 p((1+\epsilon)M_0, \Xi)$ . It follows that D is positively invariant

by the exhaust dynamics (5). The symmetric part of the Jacobian of f is

$$J_{f_{\Xi}}^{+}(M) = \frac{1}{N_{e}} \\ \begin{bmatrix} p(M_{T}, \Xi) + M_{T}p'(M_{T}, \Xi) & \frac{1}{2}M_{air}p'(M_{T}, \Xi) \\ \frac{1}{2}M_{air}p'(M_{T}, \Xi) & p(M_{T}) \end{bmatrix}$$

Computation of its eigenvalues leads to

$$eig(J_{f_{\Xi}}^{+}(M)) = \frac{1}{N_{g}} \{ p(M_{T}, \Xi) + \frac{1}{2} p (M_{T}, \Xi) (M_{T} \pm \sqrt{M_{T}^{2} + M_{air}^{2}}) \}$$

For all  $(M_T, M_{air}) \in D$ ,

$$\frac{1 - \sqrt{2}}{2} M_T \le M_T - \sqrt{M_T^2 + M_{air}^2} \le 0$$

p is increasing,

$$D \ni M \mapsto p(M_T, \Xi) + \frac{1}{2}\dot{p}(M_T, \Xi)(M_T + \frac{1 - \sqrt{2}}{2}M_T)$$

is a strictly positive increasing function. Thus,

$$\exists J_0 \in \mathbb{R}^+ \setminus \{0\}, \text{ s.t. } \forall M \in D, J_{f_\Xi}^+(M) \ge J_0 I$$

We note  $\phi(\alpha, \alpha_0, M_0)$  the trajectory of system (5) at time  $\alpha$  with initial condition  $\phi(\alpha_0, \alpha_0, M_0) = M_0$ , and define the Poincaré map

$$P_{\alpha_0}: D\ni M_0\mapsto \phi(\alpha_0+T_0,\alpha_0,M_0)\in D$$

From [31], [32], strict positiveness of  $J_f^+$  leads to the contracting property of  $P_{\alpha_0}$ , i.e.

$$\forall (M_1, M_2) \in D,$$
  
 $\|P_{\alpha_0}(M_1) - P_{\alpha_0}(M_2)\| \le e^{-J_0 T_0} \|M_1 - M_2\|$ 

Then, from the global inversion theorem,  $P_{\alpha_0}$  has a unique fixed point,  $\bar{\phi}(\alpha_0)$  and

$$\forall (t_0, M_0) \in \mathbb{R}^+ \times D, \quad \lim_{t \to \infty} (\phi(t_0 + kT_0, 0, M_0)) = \bar{\phi}(t_0)$$

 $\bar{\phi}$  is solution of (5) and  $\bar{\phi}(T_0) = \bar{\phi}(0)$ .

Proposition 1: For every initial condition in D, system (5) converges towards a unique  $T_0$ -periodic limit cycle.

System (1)-(4) consists of System (5) with added linear equations

$$\left\{ \begin{array}{ll} N_e \frac{d\lambda_{mes}}{d\alpha} & = & \frac{1}{\tau} (\frac{M_T - M_{air}}{M_T} - \lambda_{mes}) \\ N_e \frac{d\lambda_i}{d\alpha} & = & 0 \ \forall i \in [1, \ n_{cul}] \end{array} \right.$$

Trivially, the  $\lambda_i$  are constant. On the other hand,  $\lambda_{\rm mes}$  is a one dimensional asymptotically stable linear dynamics fed by a signal converging toward a limit cycle. It follows that  $\lambda_{\rm mes}$  is also converging toward a limit cycle. The following proposition holds

Proposition 2: System (1)-(4) converges toward a  $T_0$ -periodic limit cycle for every initial condition in  $D \times [0,1]^{n_{cyl}+1}$ . This limit cycle only depends on  $\lambda_1(0),\ldots,\lambda_{n_{cyl}}(0)$ . We note this limit cycle

$$[0,T_0] \ni \alpha \mapsto x_{\text{per}}(\alpha) \in D \times [0,1]^{n_{cyl}+1}$$

#### III. OBSERVER DEFINITION

The observer under consideration is a discrete-time Kalman filter defined around the attractive  $x_{per}$  trajectory.

## A. Discrete-time reference system

We now compute a discrete approximation of System (1)-(4) by an Euler explicit scheme around the limit cycle  $x_{\rm per}$  defined in the previous section. The sample angle is  $\Delta\alpha=6^o$  and for sake of simplicity we note  $x_{\rm d}(k)\triangleq x_{\rm per}(k\Delta\alpha)$  and  $x_{1,\rm d}(k),\,x_{2,\rm d}(k)$  the first and second coordinate of  $x_{\rm d}(k)$  respectively. We define  $A_k,\,B_k$  and  $C_k$  as

$$A_k = \begin{bmatrix} \alpha_k & \beta_k \\ 0 & I_{n_{cyl}} \end{bmatrix} \in \mathcal{M}_{n_{cyl}+3, n_{cyl}+3}(\mathbb{R})$$
 (6)

where  $I_{n_{cyl}}$  is the  $n_{cyl}$ -identity matrix,

$$\alpha_k \triangleq \left[ \begin{array}{ccc} 1 - \delta d_T^{'}(x_{1,d}(k)) & 0 & 0 \\ -\delta x_{2,d}(k)p_{-}^{'}(x_{1,d}(k)) & 1 - \delta p(x_{1,d}(k)) & 0 \\ \delta \frac{x_{2,d}(k)}{x_{1,d}(k)^2} & -\delta \frac{1}{x_{1,d}(k)} & 1 - \delta \end{array} \right]$$

and

$$\beta_k \triangleq \begin{bmatrix} 0 & \dots & 0 \\ \delta d_1(k\Delta\alpha) & \dots & \delta d_{n_{cyl}}(k\Delta\alpha) \\ 0 & \dots & 0 \end{bmatrix} \in \mathcal{M}_{3,n_{cyl}}(\mathbb{R}),$$

$$D_k \triangleq \delta \sum_{i=1}^{n_{cyl}} d_i(k\Delta\alpha) \begin{bmatrix} 1 & 1 & 0 & \dots & 0 \end{bmatrix}^T \tag{7}$$

and

$$C_k \triangleq \left[ \begin{array}{cccc} \gamma_T & 0 & 0 & 0 & \dots & 0 \\ 0 & 0 & 1 & 0 & \dots & 0 \end{array} \right] \in \mathcal{M}_{2,3+n_{cyl}}(\mathbb{R}) \quad (8)$$

We define the discrete-time reference dynamics as

$$\begin{cases} x_{k+1} = A_k x_k + D_k + v_k \\ y_k = C_k x_k + w_k \end{cases}$$
 (9)

where  $(v,w) \in \mathbb{R}^{3+n_{cyl}} \times \mathbb{R}^2$  are added white noise. In particular,  $A_k$ ,  $D_k$  and  $C_k$  are  $N_0 \triangleq \frac{T_0}{\Delta \alpha}$ -periodic matrices.  $x_k$  stands for the discrete time values of

$$[ M_{T,per} \quad M_{air,per} \quad \lambda_{mes,per} \quad \lambda_{1,per} \quad \dots \quad \lambda_{n_{cyl},per} ]$$

We note  $A_*=\{A_k\}_{k\in[1,N_0]}$  and  $C_*=\{C_k\}_{k\in[1,N_0]}.$  Notice that  $A_{k+N_0}=A_k$  and  $C_{k+N_0}=C_k.$ 

## B. Time-varying prediction algorithm

We use a time-varying Kalman predictor for estimation the individual AFR. For this purpose, we introduce the system

$$\hat{x}_{k+1/k} = A_k \hat{x}_{k/k-1} + D_k + L_k (y_k - C_k \hat{x}_{k/k-1})$$
 (10)

with arbitrary chosen initial condition

$$x_{0/-1} = m_0$$

In Equation (10),  $L_k$  is the Kalman gain matrix

$$L_k = A_k P_k C_k^T (C_k P_k C_k^T + R_k)^{-1}$$
 (11)

The covariance error  $P_k = cov(x_k - \hat{x}_{k/k-1})$  is recursively computed through the discrete periodic equation (DPRE)

$$P_{k+1} = A_k P_k A_k^T + Q_k - A_k P_k C_k^T (C_k P_k C_k^T + R_k)^{-1} C_k P_k A_k^T$$
(12)

where  $P_0 = cov(x_{0/-1})$  a freely chosen definite positive initial condition. At last,  $Q_k$  and  $R_k$  are weighting matrices, to be chosen in  $\mathcal{M}_{n_{cyl}+3,n_{cyl}+3}(\mathbb{R})$  and  $\mathcal{M}_{2,2}(\mathbb{R})$  respectively.

Convergence can be proven (as in [33]) using asymptotic periodicity of trajectories and a study of an approximating discrete periodic equation through uniform observability. The classic results of Bittanti [34] are at the heart of the proof.

#### IV. EXPERIMENTAL RESULTS

#### A. Tests setup

The Kalman filter described above can be tested in simulation. For that purpose, a high frequency engine model was developed in AMESim [35]. The model includes a comprehensive combustion model, balance ODEs, thermal transfer laws, and gas mixing laws. The Diesel combustion model arises from Chmela's and Barba's approaches (see [36] and [37]). It is extended to multi-pulses injection, auto-ignition delay and incorporates EGR effect corrective terms [38] (see [39] for a complete description of the combustion model). To test our observer, we apply an injection duration trajectory. It produces offsets in injection which lead to AFR disturbances. More precisely, the injection steps have an effect on the average level of the measured AFR and introduce oscillations of the overall AFR signal as represented in Figure 2. These oscillations are the direct consequences of the individual AFR errors. During cylinder 1

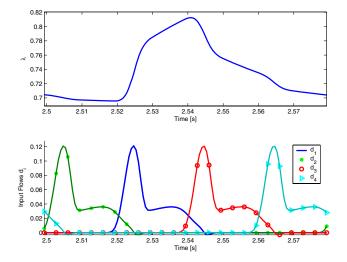


Fig. 2. AFR oscillation over 1 engine cycle during a +20% offset on cylinder 1. Top: AFR. Bottom: Cylinders output flows.

exhaust phase, the AFR increases in the manifold, and then decreases while the other cylinders exhaust phases occur. The magnitude of the oscillations is related to the amount of the AFR differences between the cylinders and the total gas mass in the manifold (and thus to its volume). The oscillations are then propagated to the turbine, and to the UEGO sensor, where it is filtered. This is the signal that we use as an input for the Kalman filter defined in Equations (10), (11), and (12).

### B. From simulation to experimentation

On the test bench, we use the proposed observer according to the scheme in Figure 3. Several practical issues need to be considered. We now detail these.

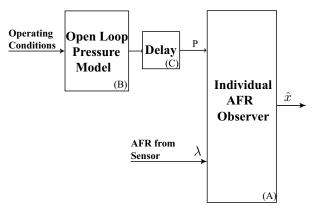


Fig. 3. Observer Scheme as used in the test bench.

1) Observer implementation: Block (A) contains the observer. The Kalman filter described in (10), (11) and (12) is extended to take into account variations of  $x_{per}$  when  $\Xi$  along varies the whole operating range in the (engine speed, load) space. Equation (10) is substituted by

$$\hat{x}_{k+1/k} = f_{\Xi}(\hat{x}_{k/k-1}) + D_k + L_k(y_k - C_k \hat{x}_{k/k-1})$$
 (13)

where the expression of  $A_k$ ,  $D_k$ ,  $C_k$ ,  $L_k$  and  $P_k$  follow their description in Section III except  $\alpha_k$  in (III-A) which becomes

$$\begin{bmatrix} 1 - \delta d_T'(\hat{x}_1(k), \Xi) & 0 \\ -\delta \hat{x}_2(k) p'(\hat{x}_1(k), \Xi) & 1 - \delta p(\hat{x}_1(k), \Xi) \end{bmatrix}$$

Initial conditions and (diagonal) weighting matrices ( $R_k$  and  $Q_k$ ) are chosen according to preliminary simulations based on the Kalman filter presented in Section III.

- 2) Open loop pressure model: Exhaust pressure sensor can be expected for forthcoming HCCI vehicles only. In experimentation, we consider not having this sensor and give to the estimator an open loop value. This value is given by the open loop balance with the input flows  $(d_i)$  and output flow  $d_T$  as described previously in Section II. This model is implemented in Block (B) in Figure 3.
- 3) Gas transport delay: Lags due to gas transport along the engine exhaust (pipes and dead volumes), and the dead time of the sensor are not represented by the model described above in System (1), (2), and (3). Delays can be lumped into a single delay for the complete exhaust system, and the model can be inverted. This delay can be identified and kept as a constant for a given setpoint on the (engine speed, IMEP (Indicated Mean Effective Pressure)) map. This estimation is implemented in Block (C) in Figure 3.

$N_e$	IMEP	$100 \ \lambda_*\ _{\infty}$	$100 \ \lambda_*\ _{\text{mean}}$
1500	3	15.9154	6.4867
1500	6	7.6264	2.11
1500	9	11.2945	3.7399
2500	6	11.4955	3.2945
2500	9	16.1126	4.5097
3500	9	20.3286	5.5793

TABLE II

Table of experimental results of the extended Kalman filter. 
$$\|\lambda_*\|_{\infty} \triangleq \max_{i,\alpha} \left| \frac{\hat{\lambda}_i - \lambda_{i,ref}}{\lambda_{i,ref}} \right| \text{ and } \|\lambda_*\|_{\text{mean}} \triangleq \max_{i,\alpha} \left| \frac{\hat{\lambda}_i - \lambda_{i,ref}}{\lambda_{i,ref}} \right|$$

## C. Experimental results

We apply the same injection duration trajectories from simulation to the test bench. The test bench under consideration is a 4 cylinders DI engine with a Variable Geometry Turbocharger (VGT) (see [39] for a complete description). Results are given in Figure 4 around an operating point (Engine Speed 1500 rpm, IMEP 9 bar). The same tuning parameters are kept from simulation to experimentation. Further, a single set of tuning parameters is kept over all operating points.

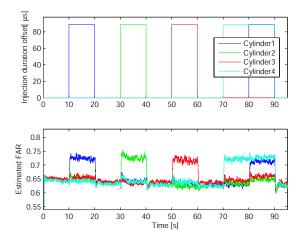


Fig. 4. Test bench results (Engine Speed  $1500 \mathrm{rpm}$ , IMEP 9bar). Top: injection duration offsets (+20%). Bottom: estimated individual AFR

Actual FAR are not directly available but can be correlated on the experimental engine to the torque produced by each cylinder (reconstructed from the experimental individual incylinder pressure sensors). These correlated values, noted  $\lambda_{ref}$ , serve as reference for comparisons. Extensive test campaign range from 1250 rpm to 3500 rpm and from 3 to 9 bar of IMEP. Tests results are reported in Table II using two standard norms. Results appears quantitatively and qualitatively satisfactory over the considered range. Results are quantitatively and qualitatively accurate. We reproduce well the evolution of the FAR. In practice, 90% convergence is achieved within 4 engine cycles. In all test bench cases, we were able to predict the individual cylinder FAR well.

Further, we can easily detect the AFR unbalance and have a good estimation of the peaks of the AFR disturbances. The magnitude of the estimated individual AFR offsets are satisfactory. Diagnosis and closed loop control strategies can be derived from this information as demonstrated in the next section.

## D. Closed loop control example

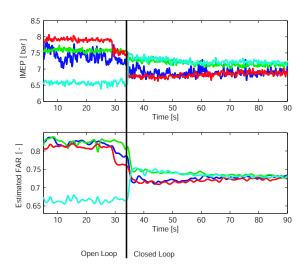


Fig. 5. Torque balancing based on individual FAR estimation: test bench results (Engine Speed 1500rpm, IMEP 7bar). We turn on the control at 34s to overcome the natural unbalance of the engine. Top: IMEP from cylinder pressure sensors. Bottom: Individual Estimated FAR with the nonlinear observer

Simple issues such as control of AFR imbalance between the cylinders can be addressed by controlling the individual injection quantities with a PI controller. Figure 5 reports the results of such a control strategy relying on the individual FAR estimation. We turn on the control at 34s and achieve tracking within a few engine cycles (10 for a 95% convergence).

## V. CONCLUSIONS AND FUTURE DIRECTIONS

This paper reports the development and implementation of an individual cylinder AFR estimator. Reconstruction of the FAR from a global oxygen concentration measurement made by a *single* sensor located downstream the turbine. This information could pave the road to efficient closed loop control strategy as demonstrated on an experimental example. Its main difference with other technics proposed in the literature is that the estimation is achieved at the highest available rate: every  $6^{\circ}$  crankshaft angle. Real-time can be achieved provided the embedded CPU can handle a  $n_{cyl}+3$  dimensional Kalman filter (typically an MPC 255 can). Availability of such an estimator giving reliable information can lead to improvements on Diesel engines in terms of combustion control, noise, and pollutant emissions.

This observer is easily transposed to various engine speeds and loads. Its dynamics are expressed in angular time scale and do not require any model for the combustion process. Theoretically, the gains do not need to be updated when the set-point is changed. However, noise is not completely set-point independent, so in practice some re-tuning may be required. At last, we need to integrate the exhaust gas recirculation flow (EGR) in the balance equation for HCCI engines. We are currently investigating this point in a campaign on the test bench.

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